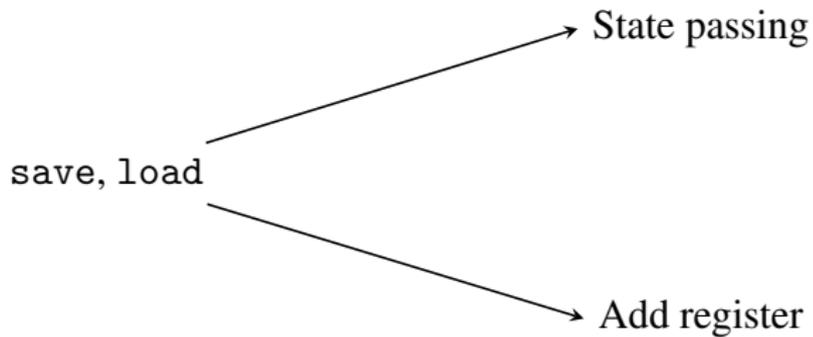
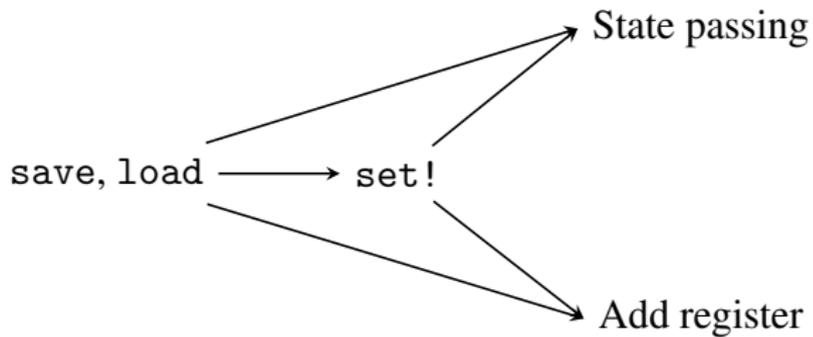


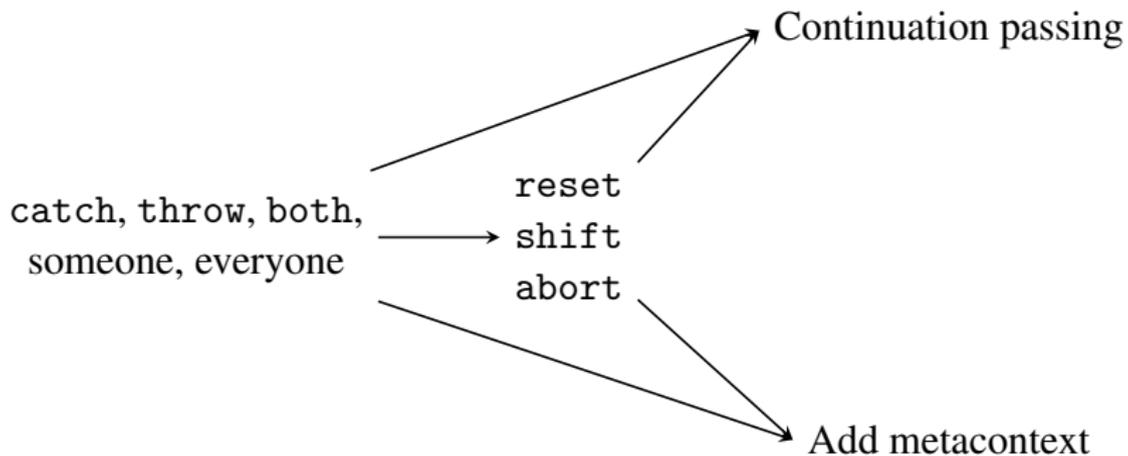
Cheating?



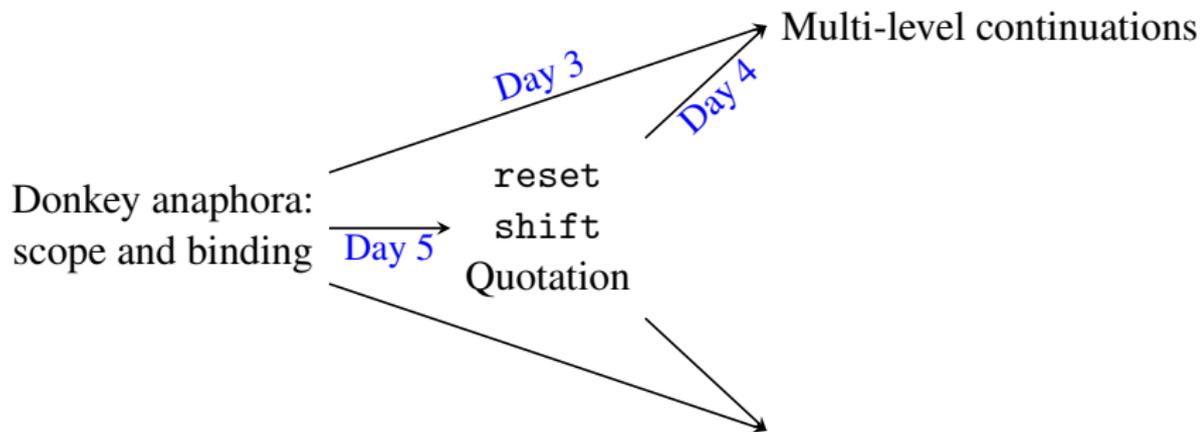
Cheating?



Cheating?



The rest of this course



Donkey anaphora is in-scope binding

Chris Barker and Chung-chieh Shan

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Donkey anaphora

If a donkey eats, it sleeps.
Every farmer who owns a donkey beats it.

Donkey anaphora

If a donkey eats, **it** sleeps.

Every farmer who owns a donkey beats **it**.

A *donkey pronoun* is a pronoun that lies outside the antecedent of a conditional (or the restrictor of a quantifier) yet covaries with an indefinite (or some other quantifier) inside it.

Donkey anaphora

If a donkey eats, it sleeps.
Every farmer who owns a donkey beats it.

A *donkey pronoun* is a pronoun that lies outside **the antecedent of a conditional (or the restrictor of a quantifier)** yet covaries with an indefinite (or some other quantifier) inside **it**.

Donkey anaphora is in-scope binding

If a donkey eats, it sleeps.
Every farmer who owns a donkey beats it.

A *donkey pronoun* is a pronoun that lies outside the antecedent of a conditional (or the restrictor of a quantifier) yet covaries with an indefinite (or some other quantifier) inside it.

Our claim: the indefinite takes scope over and binds the donkey pronoun *as usual*.

Every boy loves his mother.

Why not?

Quantifier scope is clause-bound? But not indefinites.

A donkey eats. It sleeps.

Why not?

Quantifier scope is clause-bound? But not indefinites.

A donkey eats. It sleeps.

Binding requires c-command? Just evaluation order.

Every boy's mother loves him.

Why not?

Quantifier scope is clause-bound? But not indefinites.

A donkey eats. It sleeps.

Binding requires c-command? Just evaluation order.

Every boy's mother loves him.

How to get the right truth conditions?

not $\exists d. (\mathbf{donkey} d) \wedge ((\mathbf{eats} d) \rightarrow (\mathbf{sleeps} d))$

Why not?

Quantifier scope is clause-bound? But not indefinites.

A donkey eats. It sleeps.

Binding requires c-command? Just evaluation order.

Every boy's mother loves him.

How to get the right truth conditions?

not $\exists d. (\mathbf{donkey} \ d) \wedge ((\mathbf{eats} \ d) \rightarrow (\mathbf{sleeps} \ d))$

but $\neg \exists d. (\mathbf{donkey} \ d) \wedge (\mathbf{eats} \ d) \wedge \neg(\mathbf{sleeps} \ d)$

A donkey takes scope over the entire conditional but under *if*.

A donkey sleeps if it eats.

Our account

Compositional truth conditions: *if, every, most, usually*, strong/weak.

Key: multiple levels of continuations

Plan: Everyone loves someone. (surface scope)

Everyone loves his mother.

If a donkey eats, it sleeps.

Our account

Compositional truth conditions: *if, every, most, usually*, strong/weak.

Key: **multiple levels** of continuations

Plan: Everyone loves someone. (surface scope)

Everyone loves his mother.

If a donkey eats, it sleeps.

Everyone loves someone. (inverse scope)

If a farmer owns a donkey, he beats it.

Every farmer who owns a donkey beats it.

Most farmers who own a donkey beat it.

A	Lift	$B // (A \setminus B)$
<i>expression</i>	\implies	<i>expression</i>
x		$\lambda c. c(x)$

$$\begin{array}{ccc}
 A & \text{Lift} & B // (A \setminus B) \\
 \text{expression} & \implies & \text{expression} \\
 x & & \lambda c. c(x)
 \end{array}$$

$$\begin{array}{ccc}
 C // ((A/B) \setminus D) & D // (B \setminus E) & \\
 \text{left} & \text{right} & \implies \\
 L & R & C // (A \setminus E) \\
 & & \text{left right} \\
 & & \lambda c. L(\lambda f. R(\lambda x. c(fx)))
 \end{array}$$

$$\begin{array}{ccc}
 A & \text{Lift} & B // (A \setminus B) \\
 \text{expression} & \implies & \text{expression} \\
 x & & \lambda c. c(x)
 \end{array}$$

$$\begin{array}{ccc}
 C // ((A/B) \setminus D) & D // (B \setminus E) & \implies & C // (A \setminus E) \\
 \text{left} & \text{right} & & \text{left right} \\
 L & R & & \lambda c. L(\lambda f. R(\lambda x. c(fx)))
 \end{array}$$

$$\begin{array}{ccc}
 C // (B \setminus D) & D // ((B \setminus A) \setminus E) & \implies & C // (A \setminus E) \\
 \text{left} & \text{right} & & \text{left right} \\
 L & R & & \lambda c. L(\lambda x. R(\lambda f. c(fx)))
 \end{array}$$

$$\begin{array}{ccccc}
 A & \text{Lift} & B // (A \setminus B) & A // (S \setminus S) & \text{Lower} & A \\
 \text{expression} & \implies & \text{expression} & \text{expression} & \implies & \text{expression} \\
 x & & \lambda c. c(x) & F & & F(\lambda x. x)
 \end{array}$$

$$\begin{array}{ccc}
 C // ((A/B) \setminus D) & D // (B \setminus E) & \\
 \text{left} & \text{right} & \\
 L & R & \implies C // (A \setminus E) \\
 & & \text{left right} \\
 & & \lambda c. L(\lambda f. R(\lambda x. c(fx)))
 \end{array}$$

$$\begin{array}{ccc}
 C // (B \setminus D) & D // ((B \setminus A) \setminus E) & \\
 \text{left} & \text{right} & \\
 L & R & \implies C // (A \setminus E) \\
 & & \text{left right} \\
 & & \lambda c. L(\lambda x. R(\lambda f. c(fx)))
 \end{array}$$

Linear notation	Tower notation
$B // (A \setminus C)$	$\frac{B C}{A}$
$S // (DP \setminus S)$	$\frac{S S}{DP}$

Linear notation	Tower notation
$B // (A \setminus C)$	$\frac{B C}{A}$
$S // (DP \setminus S)$	$\frac{S S}{DP}$
$\lambda c. f[c(x)]$	$\frac{f[]}{x}$
$\lambda c. \neg \exists x. c(\mathbf{mother} x)$	$\frac{\neg \exists x. []}{\mathbf{mother} x}$

$$\begin{array}{ccccc}
 A & \text{Lift} & B // (A \setminus B) & A // (S \setminus S) & \text{Lower} & A \\
 \text{expression} & \implies & \text{expression} & \text{expression} & \implies & \text{expression} \\
 x & & \lambda c. c(x) & F & & F(\lambda x. x)
 \end{array}$$

$$\begin{array}{ccc}
 C // ((A/B) \setminus D) & D // (B \setminus E) & \\
 \text{left} & \text{right} & \\
 L & R & \implies \\
 & & C // (A \setminus E) \\
 & & \text{left right} \\
 & & \lambda c. L(\lambda f. R(\lambda x. c(fx)))
 \end{array}$$

$$\begin{array}{ccc}
 C // (B \setminus D) & D // ((B \setminus A) \setminus E) & \\
 \text{left} & \text{right} & \\
 L & R & \implies \\
 & & C // (A \setminus E) \\
 & & \text{left right} \\
 & & \lambda c. L(\lambda x. R(\lambda f. c(fx)))
 \end{array}$$

$$\begin{array}{ccccc}
 & & \frac{B|B}{A} & & \frac{A|S}{S} \\
 A & \text{Lift} & A & & \text{Lower} & A \\
 \text{expression} & \implies & \text{expression} & & \text{expression} & \implies & \text{expression} \\
 x & & \frac{[]}{x} & & \frac{f[]}{x} & & f[x]
 \end{array}$$

$$\begin{array}{ccc}
 \frac{C|D}{A/B} & \frac{D|E}{B} & \frac{C|E}{A} \\
 \text{left} & \text{right} & \implies \text{left right} \\
 \frac{g[]}{f} & \frac{h[]}{x} & \frac{g[h[]]}{f(x)}
 \end{array}$$

$$\begin{array}{ccc}
 \frac{C|D}{B} & \frac{D|E}{B \setminus A} & \frac{C|E}{A} \\
 \text{left} & \text{right} & \implies \text{left right} \\
 \frac{g[]}{x} & \frac{h[]}{f} & \frac{g[h[]]}{f(x)}
 \end{array}$$

$$\begin{array}{c}
 \frac{A}{\text{expression}} \\
 x
 \end{array}
 \quad
 \text{Lift}
 \quad
 \Rightarrow
 \quad
 \frac{\frac{B|B}{A}}{\text{expression}} \\
 x$$

$$\frac{\frac{A|S}{S}}{\text{expression}}
 \quad
 \text{Lower}
 \quad
 \Rightarrow
 \quad
 \frac{A}{\text{expression}} \\
 f[x]$$

$$\frac{\frac{C|D}{A/B}}{\text{left}}
 \quad
 \frac{\frac{D|E}{B}}{\text{right}}
 \quad
 \Rightarrow
 \quad
 \frac{\frac{C|E}{A}}{\text{left right}} \\
 \frac{g[]}{f}
 \quad
 \frac{h[]}{x}
 \quad
 \frac{g[h[]]}{f(x)}$$

$$\frac{\frac{C|D}{B}}{\text{left}}
 \quad
 \frac{\frac{D|E}{B \setminus A}}{\text{right}}
 \quad
 \Rightarrow
 \quad
 \frac{\frac{C|E}{A}}{\text{left right}}
 \quad
 \frac{DP \triangleright B|B}{DP} \\
 \frac{g[]}{x}
 \quad
 \frac{h[]}{f}
 \quad
 \frac{g[h[]]}{f(x)}
 \quad
 \frac{he}{\lambda y. []} \\
 y$$

$\frac{A}{\text{expression}}$	Lift	$\frac{B B}{A}$	\implies	$\frac{A}{\frac{[]}{x}}$	Lower	$\frac{A S}{S}$	\implies	$\frac{A}{\text{expression}}$
x		x		x		x		$f[x]$

$\frac{C D}{A/B}$	$\frac{D E}{B}$	\implies	$\frac{C E}{A}$	$\frac{A B}{DP}$	Bind	$\frac{A DP \triangleright B}{DP}$
<i>left</i>	<i>right</i>		<i>left right</i>	<i>expression</i>		<i>expression</i>
$\frac{g[]}{f}$	$\frac{h[]}{x}$		$\frac{g[h[]]}{f(x)}$	$\frac{f[]}{x}$		$\frac{f([]x)}{x}$

$\frac{C D}{B}$	$\frac{D E}{B \setminus A}$	\implies	$\frac{C E}{A}$	$\frac{DP \triangleright B B}{DP}$
<i>left</i>	<i>right</i>		<i>left right</i>	<i>he</i>
$\frac{g[]}{x}$	$\frac{h[]}{f}$		$\frac{g[h[]]}{f(x)}$	$\frac{\lambda y. []}{y}$

$\frac{A}{\text{expression}}$	Lift	$\frac{B B}{A}$	$\frac{A S}{S}$	Lower	$\frac{A}{\text{expression}}$
\implies		\implies		\implies	
x		$\frac{[]}{x}$	$\frac{f[]}{x}$		$f[x]$

$\frac{C D}{A/B}$	$\frac{D E}{B}$	\implies	$\frac{C E}{A}$	$\frac{A B}{DP}$	Bind	$\frac{A DP \triangleright B}{DP}$
$left$	$right$		$left\ right$	$expression$	\implies	$expression$
$\frac{g[]}{f}$	$\frac{h[]}{x}$		$\frac{g[h[]]}{f(x)}$	$\frac{f[]}{x}$		$\frac{f([x])}{x}$

$\frac{C D}{B}$	$\frac{D E}{B \setminus A}$	\implies	$\frac{C E}{A}$	$\frac{DP \triangleright B B}{DP}$	$\frac{S S}{(S/S)/S}$
$left$	$right$		$left\ right$	he	if
$\frac{g[]}{x}$	$\frac{h[]}{f}$		$\frac{g[h[]]}{f(x)}$	$\frac{\lambda y. []}{y}$	$\frac{\neg []}{\lambda p \lambda q. p \wedge \neg q}$

Every farmer who owns a donkey beats it

$$\frac{\frac{S \mid S}{N} \quad \text{farmer who owns a donkey}}{\exists y. (\mathbf{donkey} \ y) \wedge []}}{\lambda z. (\mathbf{farmer} \ z) \wedge (\mathbf{owns} \ y \ z)}$$

Every farmer who owns a donkey beats it

$$\frac{\frac{S \mid DP \triangleright S}{N}}{\textit{farmer who owns a donkey}}}{\exists y. (\mathbf{donkey} \ y) \wedge ([\] \ y)} \frac{}{\lambda z. (\mathbf{farmer} \ z) \wedge (\mathbf{owns} \ y \ z)}$$

Every farmer who owns a donkey beats it

$$\left(\begin{array}{c} \frac{S \mid S}{S \mid S} / \frac{DP}{N} \\ \textit{every} \\ \neg \exists x. [] \\ \hline \lambda P. \frac{Px \wedge \neg []}{x} \end{array} \quad \begin{array}{c} \frac{S \mid DP \triangleright S}{N} \\ \textit{farmer who owns a donkey} \\ \exists y. (\mathbf{donkey} \ y) \wedge ([] \ y) \\ \hline \lambda z. (\mathbf{farmer} \ z) \wedge (\mathbf{owns} \ y \ z) \end{array} \right)$$

Every farmer who owns a donkey beats it

$$\left(\begin{array}{c}
 \frac{S \mid S}{S \mid S / N} \\
 \frac{DP}{\text{every}} \\
 \frac{\neg \exists x. []}{\lambda P. \frac{Px \wedge \neg []}{x}}
 \end{array} \quad
 \begin{array}{c}
 \frac{S \mid DP \triangleright S}{N} \\
 \text{farmer who owns a donkey} \\
 \frac{\exists y. (\mathbf{donkey} y) \wedge ([] y)}{\lambda z. (\mathbf{farmer} z) \wedge (\mathbf{owns} y z)}
 \end{array} \right)
 \begin{array}{c}
 \frac{DP \triangleright S \mid S}{S \mid S} \\
 \frac{DP \setminus S}{\text{beats it}} \\
 \frac{\lambda w. []}{[]} \\
 \frac{[]}{\mathbf{beats} w}
 \end{array}$$

Every farmer who owns a donkey beats it

$$\left(\begin{array}{c} \frac{S \mid S}{S \mid S} / N \\ \frac{DP}{\text{every}} \\ \frac{\neg \exists x. []}{\lambda P. \frac{Px \wedge \neg []}{x}} \end{array} \quad \begin{array}{c} \frac{S \mid DP \triangleright S}{N} \\ \text{farmer who owns a donkey} \\ \frac{\exists y. (\mathbf{donkey} y) \wedge ([] y)}{\lambda z. (\mathbf{farmer} z) \wedge (\mathbf{owns} y z)} \end{array} \right) \quad \begin{array}{c} \frac{DP \triangleright S \mid S}{S \mid S} \\ \frac{DP \setminus S}{\text{beats it}} \\ \frac{\lambda w. []}{[]} \\ \frac{[]}{\mathbf{beats} w} \end{array}$$

$\neg \exists x \exists y. \mathbf{donkey} y \wedge ((\mathbf{farmer} x \wedge \mathbf{owns} y x) \wedge \neg(\mathbf{beats} y x))$

Most farmers who own a donkey beat it

$$\begin{array}{c}
 \frac{S \mid S}{\frac{S \mid S}{DP} / N} \\
 \textit{most} \\
 \frac{\text{MOST}(\lambda x \lambda p. [])}{\lambda P. \frac{Px \wedge (p \vee [])}{x}}
 \end{array}$$

$$\text{MOST}(F) = \left(\frac{\#\{x \mid F(x)(\text{FALSE})\}}{\#\{x \mid F(x)(\text{TRUE})\}} > \frac{1}{2} \right)$$

Most farmers who own a donkey beat it (**weak**)

$$\frac{\frac{\frac{S \mid S}{DP} / N}{most}}{MOST(\lambda x \lambda p. [])}$$

$$\lambda P. \frac{Px \wedge (p \vee [])}{x}$$

$$MOST(F) = \left(\frac{\#\{x \mid F(x)(FALSE)\}}{\#\{x \mid F(x)(TRUE)\}} > \frac{1}{2} \right)$$

Most farmers who own a donkey beat it (**strong**)

$$\frac{\frac{\frac{S \mid S}{DP} / N}{most}}{MOST(\lambda x \lambda p. [])}$$

$$\lambda P. \frac{Px \wedge (p \vee \neg [])}{x}$$

$$MOST(F) = \left(\frac{\#\{x \mid F(x)(FALSE)\}}{\#\{x \mid F(x)(TRUE)\}} < \frac{1}{2} \right)$$